

9-3 (1)  $\lambda = \frac{u}{f} = \frac{80 \text{ cm/s}}{10 \text{ Hz}} = 8 \text{ cm}$

(2)  $y = A \cos(\omega t + \varphi)$  有  $t=0$  时  $y=0, \dot{y}>0$ , 不妨  $\varphi=0$

$y = 2 \cos\left(20\pi t - \frac{\pi}{2}\right) \text{ cm}$  (t 单位 s)

(3) 波方程:  $y = A \sin(\omega t - kx + \varphi)$  其中  $k = \frac{2\pi}{\lambda}$

$y = 2 \sin\left[2\pi\left(10t - \frac{x}{8}\right) - \frac{\pi}{2}\right] \text{ cm}$  (t, x 单位 s, cm)

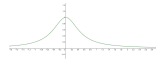
(4)  $x_1 = 4 \text{ cm}$  处  $\Delta\varphi = -k\Delta x = -\frac{2\pi}{8} \Delta x = -\pi$   $\varphi' = \varphi + \Delta\varphi = -\frac{3}{2}\pi$

9-5 (1)  $x_1 < x_2$ ,  $x_2$  处相位落后于  $x_1$  ( $x_2 - x_1 < \lambda$ ) 故向 x 负方向传播

(2)  $\Delta\varphi = k(x_2 - x_1)$  其中  $k = \frac{2\pi}{\lambda}$ , 故  $\lambda = \frac{2\pi}{\Delta\varphi}(x_2 - x_1) = 24 \text{ cm} = 0.24 \text{ m}$

$v = \lambda \cdot f = 48 \text{ cm/s} = 0.48 \text{ m/s}$

9-8 (1)  $b=1, u=1$



(2)  $y(x, t) = f\left(x - \frac{u}{2}t\right)$ , 速率为  $\frac{u}{2}$ , 沿 x 正向传播

(3)  $v(x) = \left. \frac{\partial y(x, t)}{\partial t} \right|_{t=0} = \frac{2b^3 u (2x - ut)}{[b^2 + (2x - ut)^2]^2} \Big|_{t=0} = \frac{4b^3 x u}{(b^2 + 4x^2)^2}$  (y 正向)

9-11 (1)  $v_{p1} = \frac{\omega_1}{k_1} = 1.2 \text{ m/s}$   $v_{p2} = \frac{\omega_2}{k_2} = 1.25 \text{ m/s}$

(2)  $y = y_1 + y_2 = A \cos(6t - 5\pi x) + A \cos(5t - 4\pi x) = 2A \cos\left(\frac{1}{2}t - \frac{1}{2}\pi x\right) \cos\left(\frac{11}{2}t - \frac{9}{2}\pi x\right)$

相邻振幅为 0 的距离  $\Delta x = \frac{\lambda_2}{2} = \frac{\pi}{\frac{1}{2}(\text{m}^{-1})} = 2\pi \text{ m}$

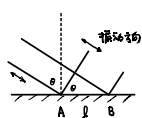
(3)  $v_g = \frac{\frac{1}{2} \text{ s}^{-1}}{\frac{1}{2} \text{ m}^{-1}} = 1 \text{ m/s}$

9-12 (1)  $\frac{B}{A} = \left| \frac{u_1 - u_2}{u_1 + u_2} \right| = \frac{1}{3}$ , 其中  $u_1 = \sqrt{\frac{T}{\rho_1}}$ ,  $u_2 = \sqrt{\frac{T}{\rho_2}}$

得  $\frac{\rho_2}{\rho_1} = 4$  或  $\frac{1}{4}$

(2)  $\frac{C}{A} = \frac{2 \cdot u_1}{u_1 + u_2} = \frac{2}{1 + \sqrt{\frac{\rho_2}{\rho_1}}} = \frac{2}{3}$  或  $\frac{3}{4}$

9-14

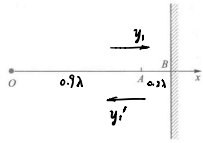


入射纵波与反射横波 振动方向相同, 如图, 界面上 A, B 为两次波源, 距离 l

纵波 B 落后 A:  $\frac{l \sin \theta}{u_p}$  横波 B 超前 A:  $\frac{l \cos \theta}{u_s}$

有  $\frac{l \sin \theta}{u_p} = \frac{l \cos \theta}{u_s}$  从而  $\theta = \arctan \frac{u_p}{u_s} = \frac{\pi}{3}$

9-19



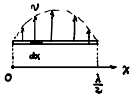
题 9-19 图

(1) 入射波  $y_1 = A \cos \left[ \omega t + 0.2\pi - k(\pi - 0.7\lambda) \right] = A \cos \left( \omega t - \frac{2\pi}{\lambda} x \right)$

(2) 反射波  $y_1' = A \cos \left[ \omega t - k(2.2\lambda - x) + \pi \right] = A \cos \left( \omega t + \frac{2\pi}{\lambda} x + 0.6\pi \right)$

(3) 合成驻波  $y = y_1 + y_1' = A \cos \left( \omega t - \frac{2\pi}{\lambda} x \right) + A \cos \left( \omega t + \frac{2\pi}{\lambda} x + 0.6\pi \right)$   
 $= 2A \cos \left( \frac{2\pi}{\lambda} x + 0.3\pi \right) \cos \left( \omega t + 0.3\pi \right)$

9-20



取位移为 0 时刻，相邻波节点能量  $E = E_k$ ， $x$  处  $dx$  元微元动能为  $dE_k$

$dE_k = \frac{1}{2} \rho v^2 dx$  其中  $v = 2\omega A \sin \frac{2\pi}{\lambda} x$

故相邻波节点能量  $E = E_k = \int_0^{\lambda/2} \frac{1}{2} \rho (2\omega A \sin \frac{2\pi}{\lambda} x)^2 dx = \frac{1}{2} \rho \omega^2 \lambda A^2 = 6.3165 \times 10^{-2} \text{ J}$

9-21

弦线上的横波波动方程： $\frac{\partial^2 y}{\partial t^2} - \sqrt{\frac{T}{\rho}} \frac{\partial^2 y}{\partial x^2} = 0$  故波速： $u = \sqrt{\frac{T}{\rho}}$  波长： $\lambda = \frac{u}{f}$

形成  $k$  个波腹的驻波： $l = k \cdot \frac{\lambda}{2}$

由上述各式得： $T = \rho \left( \frac{2fl}{k} \right)^2$ ，重物质量： $m = \frac{T}{g} = \frac{\rho}{g} \left( \frac{2fl}{k} \right)^2$

代入 $k=1, 2, 3$ 得：	$k=1$	$k=2$	$k=3$
	$T=15.3 \text{ kg}$	$T=3.83 \text{ kg}$	$T=1.70 \text{ kg}$

9-22

潜艇接收频率  $f = \frac{u+v}{u} f_0$  其中  $u, v$  分别为声速和船速， $f_0$  为声的发射频率

声的接收频率  $f' = \frac{u}{u-v} f_0$  结合二式得  $f' = \frac{2u+v}{u-v} f_0$

$y = \cos(\omega t + \varphi_1) + \cos(\omega' t + \varphi_2) = 2 \cos \left( \frac{\omega + \omega'}{2} t + \varphi_1 - \varphi_2 \right) \cos \left( \frac{\omega - \omega'}{2} t + \varphi_1 + \varphi_2 \right) = A(t) \cos \left( \frac{\omega + \omega'}{2} t + \varphi_1 + \varphi_2 \right)$

强度正比于  $A^2(t) = 2 \left[ 1 - \cos((\omega - \omega')t + \varphi_1 - \varphi_2) \right]$  为  $|\omega - \omega'|$  的拍

故拍频  $f_b = f' - f_0 = \frac{2u}{u-v} f_0$  得  $v = \frac{f_b}{2f_0 + f_b} u \approx 6 \text{ m/s}$



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9-3

1)  $\lambda = \frac{u}{f} = 8 \text{ cm}$

2)  $y = 2 \sin(\omega t) \text{ (cm)}$

$\omega = 2\pi f = 20\pi \text{ rad/s}$

$\therefore y = 2 \sin(20\pi t) \text{ (cm)}$

3)  $y = 2 \sin(\omega t - kx) \text{ (cm)}$

$k = \frac{\omega}{u} = \frac{\pi}{4} \text{ cm}^{-1}$

$y = 2 \sin(20\pi t - \frac{\pi}{4}x) \text{ (cm)}$

4)  $y = 2 \cos(20\pi t - \frac{\pi}{4}x - \frac{\pi}{2}) \text{ (cm)}$

初相位  $\varphi_0 = -\frac{3}{2}\pi$

9-5

(1) 沿 x 轴正向传播

2)  $k \cdot (x_2 - x_1) = \frac{\pi}{4}$

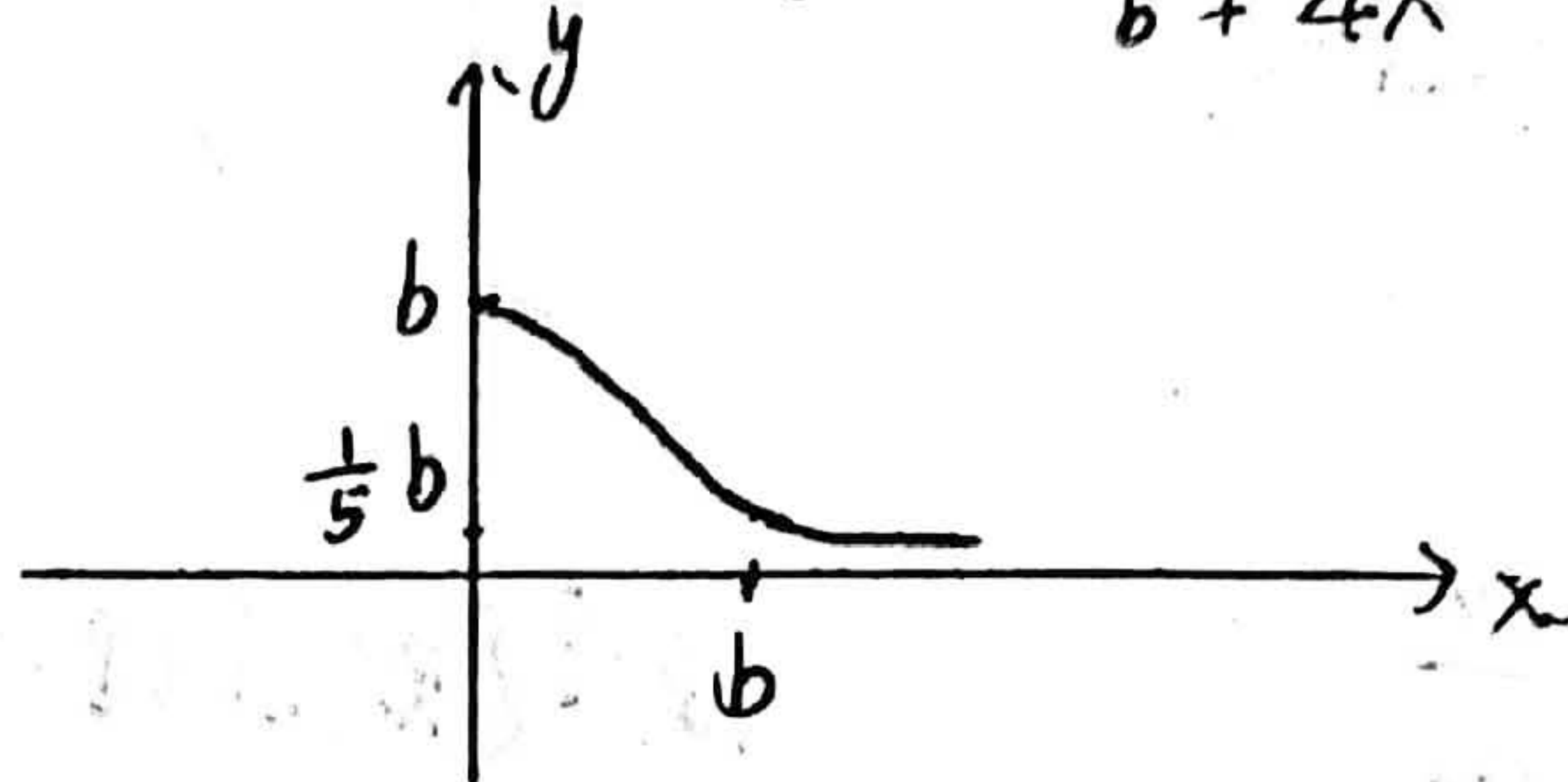
$k = \frac{\pi}{12} \text{ cm}^{-1} = \frac{2\pi}{\lambda}$

$\therefore \lambda = 24 \text{ cm}$

$v = \lambda f = 48 \text{ cm/s}$

9-8

1)  $t=0$  时  $y(x) = \frac{b^3}{b^2 + 4x^2}$



2)

$\frac{d(2x - ut)}{dt} = 0 \implies 2 \frac{dx}{dt} - u = 0$

$\frac{dx}{dt} = \frac{1}{2}u$ ,  $\therefore$  脉冲速率  $v = \frac{1}{2}u$ , 方向沿 x 正方向

3)  $\frac{\partial y}{\partial t} = -\frac{2b^3(2x-ut)(-u)}{[b^2+(2x-ut)^2]^2} = \frac{2b^3(2x-ut)u}{[b^2+(2x-ut)^2]^2}$

$\left. \frac{\partial y}{\partial t} \right|_{t=0} = \frac{4ub^3x}{(b^2+4x^2)^2}$

9-11

1)  $v_{p1} = \frac{\omega_1}{k_1} = 1.2 \text{ m/s}$

$v_{p2} = \frac{\omega_2}{k_2} = 1.25 \text{ m/s}$

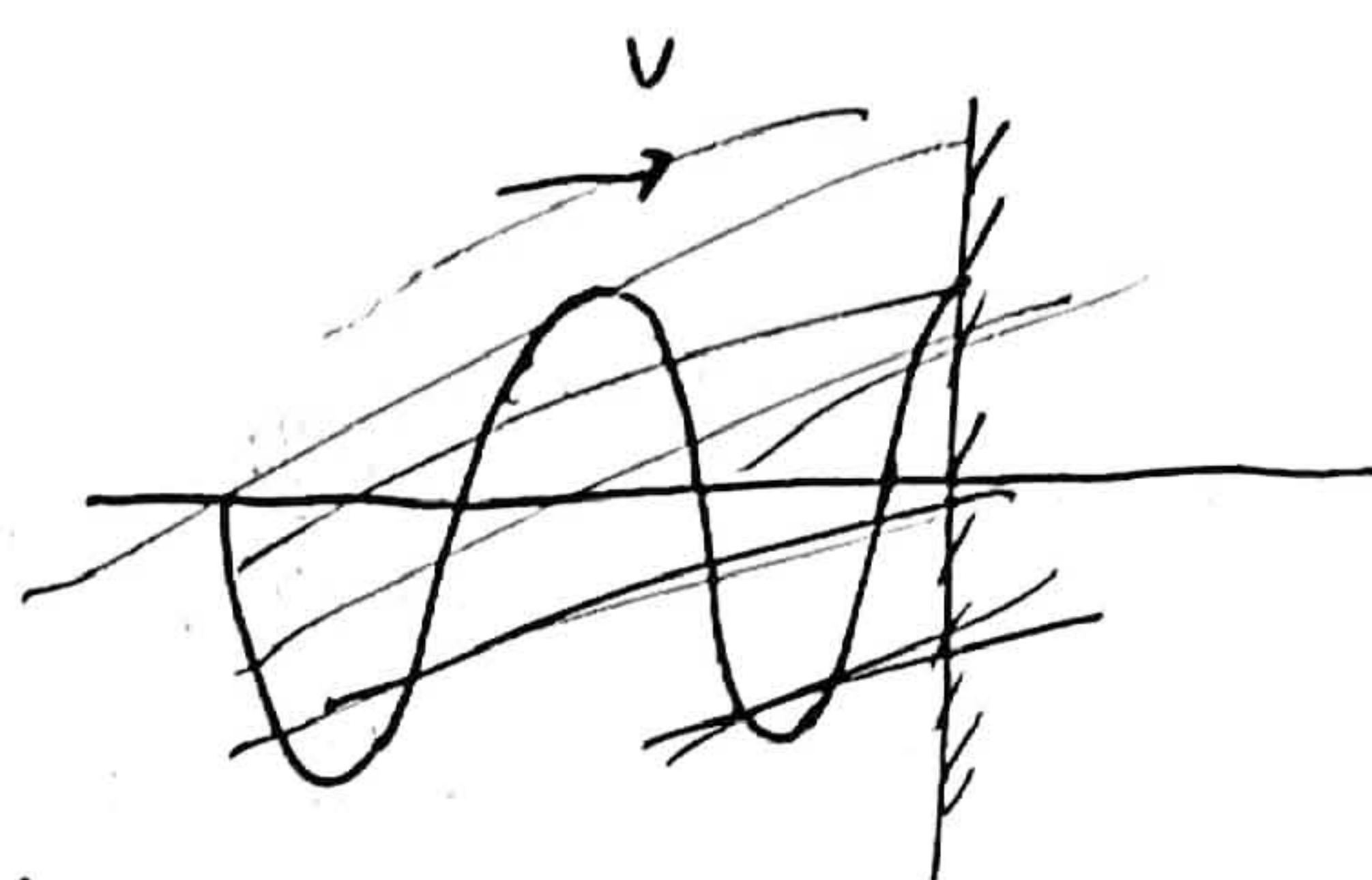
2)  $y_1 + y_2 = 2A \cos(\frac{11t - 9x}{2}) \cos(\frac{t-x}{2})$

将  $2A \cos(\frac{t-x}{2})$  一项看成振幅

相邻两点的距离  $\Delta x = 2\pi \text{ m}$

(3) 题解  $v_g = \frac{\omega}{k} = 1 \text{ m/s}$

9-14.



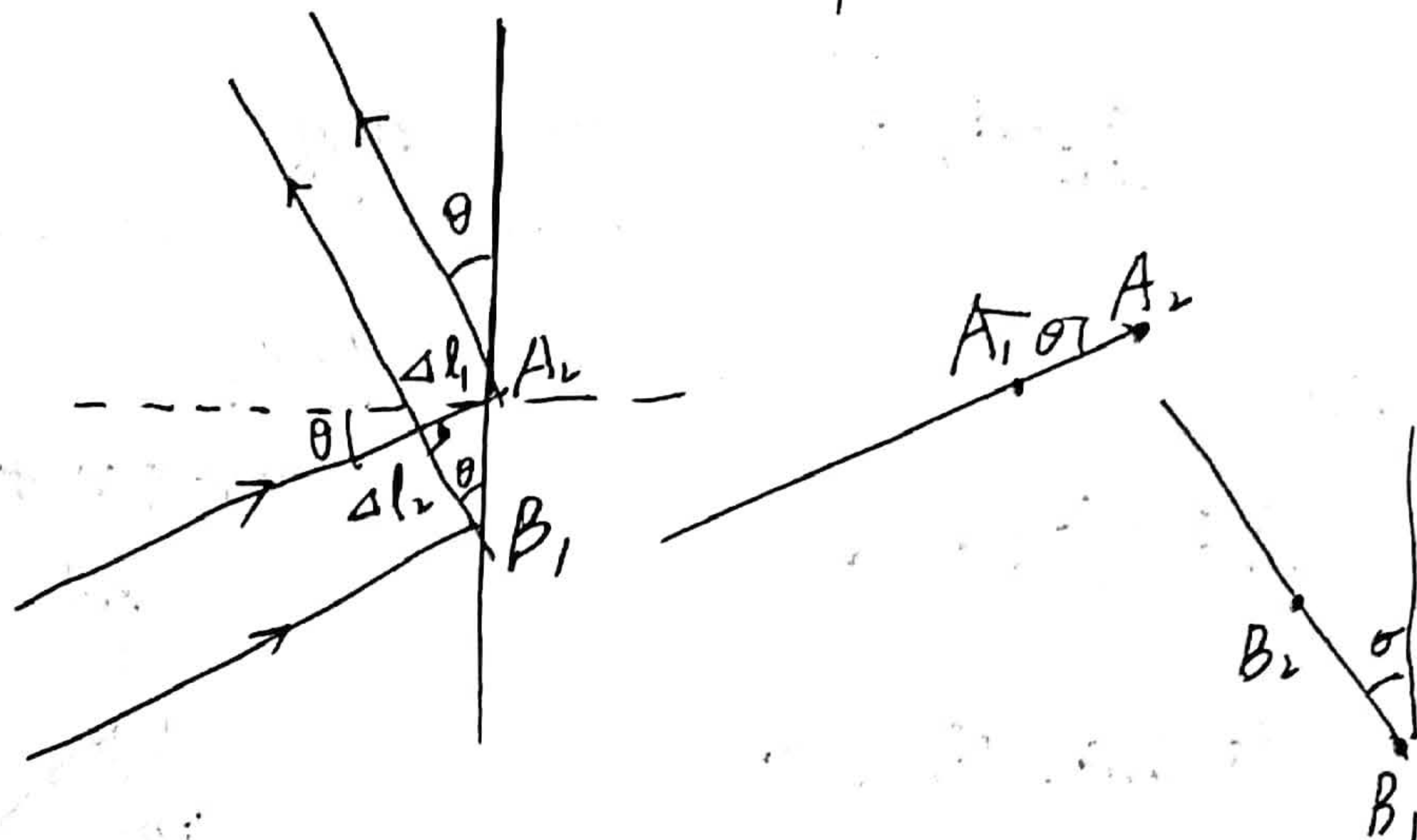
9-12.

(1).

设入射波  $y_1 = A \cos(\omega t - k_1 x)$

反射波  $y_2 = B \cos(\omega t + k_1 x + \varphi_2)$

出射波:  $y_3 = C \cos(\omega t - k_2 x + \varphi_3)$



由惠更斯原理可找到等相位的波阵面

考虑相位差  $\varphi_{A_1 A_2}, \varphi_{B_1 B_2}$

$$\varphi_{A_1 A_2} = \frac{\omega}{u_1} \cdot \Delta l_1$$

$$\varphi_{B_1 B_2} = \frac{\omega}{u_2} \cdot \Delta l_2 \quad \text{有} \quad \frac{u_1}{u_2} = \sqrt{3}$$

$$\text{又} \quad \varphi_{A_1 A_2} = \varphi_{B_1 B_2}$$

$$\text{得} \quad \frac{\Delta l_1}{\Delta l_2} = \tan \theta = \frac{u_1}{u_2} = \sqrt{3}$$

$$\therefore \theta = 60^\circ$$

满足:  $y_1 + y_2 = y_3 \quad |_{x=0}$

其中  $k_1 = \frac{\omega}{u_1}, k_2 = \frac{\omega}{u_2}$

$$u_1 = \sqrt{\frac{F_T}{\rho_{11}}}, \quad u_2 = \sqrt{\frac{F_T}{\rho_{12}}}$$

且满足:

$$-\frac{\partial(y_1 + y_2)}{\partial x} F_T \Big|_{x=0} + \frac{\partial y_3}{\partial x} F_T \Big|_{x=0} = 0$$

$$A + B \cos \varphi_2 = C \cos \varphi_3$$

$$B \sin \varphi_2 = C \sin \varphi_3$$

$$k_1 A - k_1 B \cos \varphi_2 = k_2 C \cos \varphi_3$$

$$-k_1 B \sin \varphi_2 = k_2 C \sin \varphi_3$$

且有:  $\frac{B}{A} = \frac{1}{3}$

待  $k_1 = 2k_2$  即  $\frac{\rho_{11}}{\rho_{12}} = 4$

或  $k_1 = \frac{1}{2}k_2$  即  $\frac{\rho_{11}}{\rho_{12}} = \frac{1}{4}$

(2).

若  $k_1 = 2k_2$  有:  $A + B = C \Rightarrow C = \frac{4}{3}A$

若  $k_1 = \frac{1}{2}k_2$  有:  $A - B = C \Rightarrow C = \frac{2}{3}A$



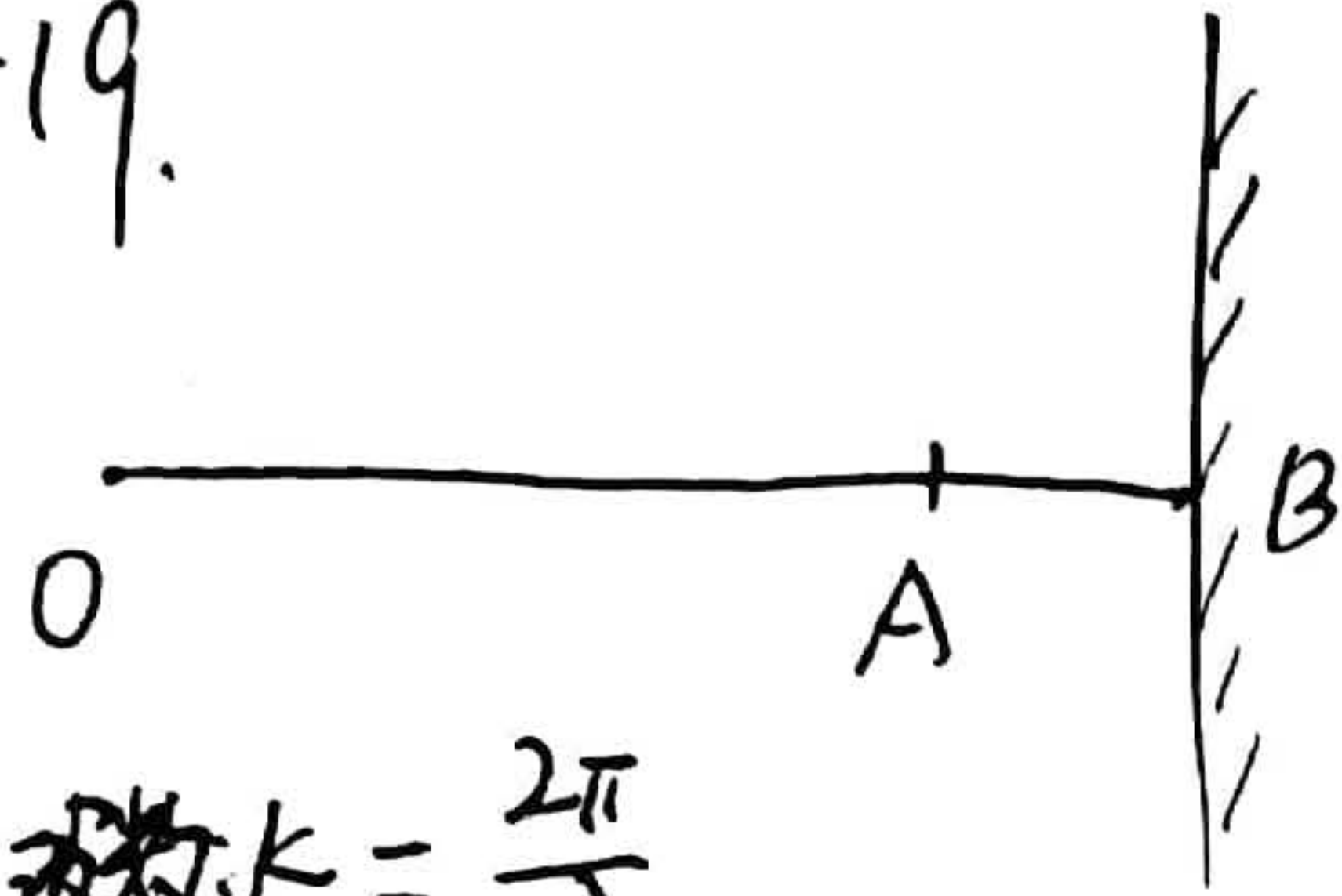
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9-19.



波数  $k = \frac{2\pi}{\lambda}$

入射波:  $y_{in} = A \cos(\omega t - k(x - 0.9\lambda) + 0.2\pi)$

$y_{in} = A \cos(\omega t - kx)$

(2).

反射波  $y_{re} = A \cos(\omega t + kx + \varphi_1)$

满足  $(y_{in} + y_{re})|_{x=1.1\lambda} = 0$

$y_{in} + y_{re} = 2A \cos(\omega t + \frac{1}{2}\varphi_1) \cos(kx + \frac{1}{2}\varphi_1)$

$\cos(1.1\lambda k + \frac{1}{2}\varphi_1) = 0$

得  $\varphi_1 = 0.6\pi$

$\therefore y_{re} = A \cos(\omega t + kx + 0.6\pi)$

(3). 驻波方程:

$y = y_{in} + y_{re} = 2A \cos(\omega t + \frac{3}{10}\pi) \cos(kx + \frac{3}{10}\pi)$

$= \frac{1}{2} \rho_1 \omega^2 A^2 \lambda$

代入数据得

$E_0 = 0.0632 \text{ J} = 6.32 \times 10^{-2} \text{ J}$

9-20.

取  $x$  处长度  $dx$  微元

其动能

$dE_k = \frac{1}{2} (\rho_1 \cdot dx) \left( \frac{\partial y}{\partial t} \right)^2$

其势能

$dE_p = \frac{1}{2} \cdot E \cdot dx \cdot \left( \frac{\partial y}{\partial x} \right)^2$

有体密度  $\rho_v \cdot S = \rho_1$

波速  $u = \frac{\omega}{k} = \sqrt{\frac{E}{\rho_v}}$

可以此为准

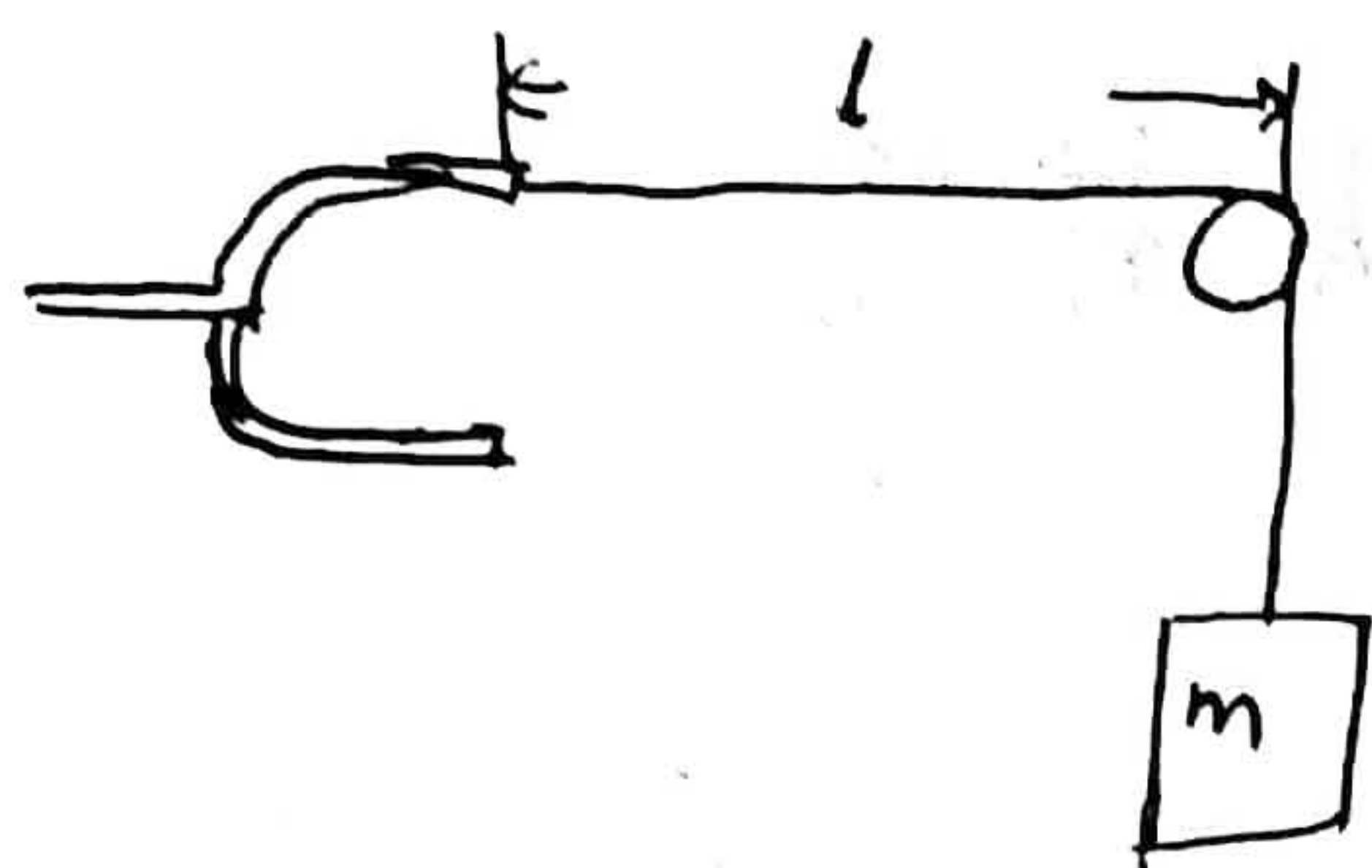
$dE_k + dE_p = 2\rho_1 \omega^2 A^2 \left[ \cos^2(\omega t + \frac{3}{10}\pi) \sin^2(kx + \frac{3}{10}\pi) + \sin^2(\omega t + \frac{3}{10}\pi) \cos^2(kx + \frac{3}{10}\pi) \right]$

$\frac{1}{2} dE = dE_k + dE_p$

$E_0 = \int_0^{E_0} dE = 2\rho_1 \omega^2 A^2 \left( \int_0^{\frac{\lambda}{2}} \cos^2(\omega t + \frac{3}{10}\pi) \sin^2(kx + \frac{3}{10}\pi) dx + \int_0^{\frac{\lambda}{2}} \sin^2(\omega t + \frac{3}{10}\pi) \cos^2(kx + \frac{3}{10}\pi) dx \right)$

$= \frac{1}{2} \rho_1 \omega^2 A^2 \lambda$

9-21.



有:  $f_2 - f_0 = \Delta f$

$\Delta f$  为拍频频率

$$v = \frac{\Delta f \cdot \lambda}{2f_0 + \Delta f} = 6.00 \text{ m/s}$$

有波传播速度:

$$u = \sqrt{\frac{F_T}{\rho l_1}} = \sqrt{\frac{mg}{\rho l_1}}$$

波长:  $\lambda = \frac{u}{f} = \frac{1}{f} \sqrt{\frac{mg}{\rho l_1}}$

波形成  $n$  个波腹

有:  $\frac{n}{2} \lambda = l$

$$m = \frac{4l_1 f^2 l^2}{n^2 g}$$

$n=1$  时,  $m=15.3 \text{ kg}$

$n=2$  时  $m=3.83 \text{ kg}$

$n=3$  时  $m=1.70 \text{ kg}$

9-27.

入射波频率为  $f_0$

设接收器接收到的频率  $f_1$ , 接收器有速度  $v$

$$f_1 = \frac{u+v}{u} f_0, \text{ 其中 } u \text{ 为波速.}$$

接收器接收频率  $f_2$

$$f_2 = \frac{u}{u-v} f_1 = \frac{u+v}{u-v} f_0$$

# 第九章作业

9-3

解: (1)  $u = 80 \text{ cm/s}$   $\nu = 10 \text{ Hz}$   $\therefore T = \frac{1}{\nu} = 0.1 \text{ s}$   $\therefore \lambda = u \cdot T = 8 \text{ cm}$ .

(2)  $\omega = 2\pi\nu = 20\pi \text{ rad/s}$

$\therefore y(0, t) = 2 \cos(20\pi t - \frac{\pi}{2}) \text{ cm}$

(3)  $\therefore y(x, t) = 2 \cos[20\pi t - \frac{2\pi}{\lambda}x - \frac{\pi}{2}] = 2 \cos[20\pi t - \frac{\pi}{4}x - \frac{\pi}{2}] \text{ cm}$

(4)  $y(4, 0) = 2 \cos(-\pi - \frac{\pi}{2}) = 2 \cos(-\frac{3}{2}\pi) \therefore \varphi' = -\frac{3}{2}\pi$

9-5

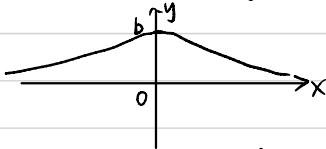
解: (1)  $\nu = 2.0 \text{ Hz}$   $\therefore \Delta\varphi = -\frac{2\pi}{\lambda} \Delta x \therefore \lambda = -2\pi \frac{\Delta x}{\Delta\varphi} = -24 \text{ cm}$

$\therefore$  沿  $x$  轴负方向

(2) 由(1)知:  $\lambda = 24 \text{ cm}$ .  $u = \lambda \cdot \nu = 48 \text{ cm/s}$

9-8

解: (1)  $t=0$  时:  $y(x, 0) = \frac{b^3}{b^2 + (2x)^2} = \frac{b^3}{b^2 + 4x^2}$



(2) 方向: 沿  $+x$  方向 设经过  $\Delta t$  时间: 波峰位置:  $2x - u\Delta t = 0 \therefore x = \frac{u}{2} \Delta t$

$\therefore$  波速:  $\frac{u}{2}$

(3)  $\therefore \frac{\partial y}{\partial t} = \frac{-b^3 \cdot 2(2x-ut)(-u)}{[b^2 + (2x-ut)^2]^2} = \frac{2b^3 u (2x-ut)}{[b^2 + (2x-ut)^2]^2}$

当  $t=0$  时  $\left. \frac{\partial y}{\partial t} \right|_{t=0} = \frac{2b^3 u \cdot 2x}{(b^2 + 4x^2)^2} = \frac{4xub^3}{(b^2 + 4x^2)^2}$

9-11

解: (1)  $\therefore v_p = v_{\text{波}}$   $\alpha \therefore \omega_1 = b \text{ rad/s} \therefore T_1 = \frac{2\pi}{\omega_1} = \frac{\pi}{3} \text{ s}$ .

$\alpha \therefore -\frac{2\pi}{\lambda_1} = -5 \therefore \lambda_1 = \frac{2\pi}{5} \text{ m} \therefore v_{\text{波}1} = \frac{\lambda_1}{T_1} = \frac{6}{5} \text{ m/s}$

$$\omega_2 = 5 \text{ rad/s} \quad T_2 = \frac{2\pi}{\omega_2} = \frac{2\pi}{5} \text{ rad/s} \quad -\frac{2\pi}{\lambda_2} = -4 \quad \therefore \lambda_2 = \frac{\pi}{2} \text{ m}$$

$$\therefore v_2 = \lambda_2 \omega_2 = \frac{\pi/2}{5} = \frac{\pi}{10} \text{ m/s} \quad \therefore v_{p2} = \frac{5}{4} \text{ m/s}$$

$$\begin{aligned} (2) \therefore y &= y_1 + y_2 = A \cos(6t - 5x) + A \cos(5t - 4x) \\ &= A \left( 2 \cos \frac{11t - 9x}{2} \cos \frac{t - x}{2} \right) \\ &= 2A \cos \frac{t - x}{2} \cos \frac{11t - 9x}{2} \end{aligned}$$

$$\therefore \text{令 } 2A \cos \frac{t - x}{2} = 0 \quad \therefore \Delta x = 2\pi \text{ (m)}$$

$$(3) v_g' = \frac{\Delta \omega}{\Delta k} = \frac{1}{1} = 1 \text{ m/s}$$

9-12

解: (1) ① 波密  $\rightarrow$  波疏:

$$Z = \rho u = \rho \sqrt{\frac{T}{\rho}} = \sqrt{TP}$$

$$\therefore A_1' = \frac{\sqrt{TP_1} - \sqrt{TP_2}}{\sqrt{TP_1} + \sqrt{TP_2}} A_1 = \frac{\sqrt{P_1} - \sqrt{P_2}}{\sqrt{P_1} + \sqrt{P_2}} A_1$$

$$\therefore \frac{B}{A} = \frac{1}{3} = \frac{\sqrt{P_1} - \sqrt{P_2}}{\sqrt{P_1} + \sqrt{P_2}} \quad \therefore P_1 = 4P_2 \quad \therefore \frac{P_{11}}{P_{12}} = 4$$

② 波疏  $\rightarrow$  波密

$$\frac{B}{A} = -\frac{1}{3} = \frac{\sqrt{P_1} - \sqrt{P_2}}{\sqrt{P_1} + \sqrt{P_2}} \quad \therefore P_2 = 4P_1 \quad \therefore \frac{P_{21}}{P_{22}} = \frac{1}{4}$$

(2) ①  $P_1 = 4P_2$  时:  $Z_1 = 2Z_2$ :

$$A_2 = \frac{2Z_1}{Z_1 + Z_2} A_1 = \frac{4Z_2}{2Z_2 + Z_2} A_1 = \frac{4}{3} A_1 \quad \therefore \frac{C}{A} = \frac{4}{3}$$

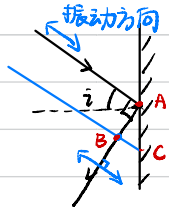
②  $P_2 = 4P_1$  时:  $Z_2 = 2Z_1$ :

$$A_2 = \frac{2Z_1}{Z_1 + Z_2} A_1 = \frac{2Z_1}{Z_1 + 2Z_1} A_1 = \frac{2}{3} A_1 \quad \therefore \frac{C}{A} = \frac{2}{3}$$



9-14

解:  $\therefore u_{\text{纵}} = \sqrt{3} u_{\text{横}} \quad \therefore z_1 = \sqrt{3} z_2$   
 $\therefore l_{BC} = u_{\text{纵}} \Delta t \quad l_{AB} = u_{\text{横}} \Delta t$   
 $\therefore \tan \bar{\nu} = \frac{l_{BC}}{l_{AB}} = \frac{u_{\text{纵}}}{u_{\text{横}}} = \sqrt{3} \quad \therefore \bar{\nu} = 60^\circ$



9-19

解: (1)  $y_A = A \cos(\omega t + 0.2\pi)$   
 $y_1 = A \cos[\omega t + 0.2\pi - \frac{2\pi}{\lambda}(x - 0.9\lambda)]$   
 $\therefore y_1 = A \cos(\omega t - \frac{2\pi}{\lambda}x)$   
 (2)  $\therefore y_1(1.1\lambda, t) = A \cos(\omega t - \frac{2\pi}{\lambda} \cdot 1.1\lambda) = A \cos(\omega t - 0.2\pi)$   
 设反射波:  $y_2(x, t) = A \cos(\omega t + \frac{2\pi}{\lambda}x + \varphi)$   
 $\therefore y_2(1.1\lambda, t) = A \cos(\omega t + 0.2\pi + \varphi)$   
 根据固定端:  $y_1(1.1\lambda, t) + y_2(1.1\lambda, t) = 0$   
 $\therefore 2A \cos \frac{2\omega t + \varphi}{2} \cos \frac{0.4\pi + \varphi}{2} = 0$

$\therefore 0.4\pi + \varphi = \pi \quad \therefore \varphi = 0.6\pi$

$\therefore y_2(x, t) = A \cos(\omega t + \frac{2\pi}{\lambda}x + 0.6\pi)$

(3) 驻波:  $y = y_1 + y_2 = A \cos(\omega t - \frac{2\pi}{\lambda}x) + A \cos(\omega t + \frac{2\pi}{\lambda}x + 0.6\pi)$   
 $= 2A \cos(\omega t + 0.3\pi) \cos(\frac{2\pi}{\lambda}x + 0.3\pi)$   
 $= 2A \cos(\frac{2\pi}{\lambda}x + 0.3\pi) \cos(\omega t + 0.3\pi)$

9-20

解:  $\begin{cases} \frac{2\pi}{\lambda}x + 0.3\pi = \frac{\pi}{2} \\ \frac{2\pi}{\lambda}x + 0.3\pi = -\frac{\pi}{2} \end{cases} \quad \therefore \begin{cases} x = 0.1\lambda \\ x = -0.4\lambda \end{cases}$

$\therefore W = \int_{-0.4\lambda}^{0.1\lambda} \frac{1}{2} \rho dx \cdot 4A^2 \omega^2 \cos^2(\frac{2\pi}{\lambda}x + 0.3\pi) = \int_{-0.4\lambda}^{0.1\lambda} PA^2 \omega^2 [\cos(\frac{4\pi}{\lambda}x + 0.6\pi) + 1] dx$   
 $= PA^2 \omega^2 [\frac{\lambda}{4\pi} \cdot 0 + 0.5\lambda] = \frac{1}{2} PA^2 \omega^2 \lambda = 6.3 \times 10^{-2} \text{ J}$

9-21

解:  $T = mg$      $T = u^2 P_e$      $u = \lambda \cdot \nu$

①  $\frac{1}{2}\lambda = l$  时     $u = 2 \times 50 = 100 \text{ m/s}$      $\therefore T = 150 \text{ N}$      $\therefore m = \frac{T}{g} = 15.3 \text{ kg}$

②  $\lambda = l$  时     $u = 1 \times 50 = 50 \text{ m/s}$      $\therefore T = 37.5 \text{ N}$      $m = 3.8 \text{ kg}$

③  $\frac{3}{2}\lambda = l$  时     $u = \frac{100}{3} \text{ m/s}$      $T = \frac{50}{3} \text{ N}$      $m = 1.7 \text{ kg}$

9-27

解: 船接收到的频率:  $\nu' = \frac{u - v_R}{u} \nu$

探测器接收到的反射波频率:  $\nu'_R = \frac{u}{u + v_R} \nu' = \frac{u - v_R}{u + v_R} \nu$

$\therefore$  拍频  $241 \text{ Hz} = |\nu - \nu'_R| = \frac{2v_R}{u + v_R} \cdot \nu$     解得:  $v_R = 6 \text{ m/s}$